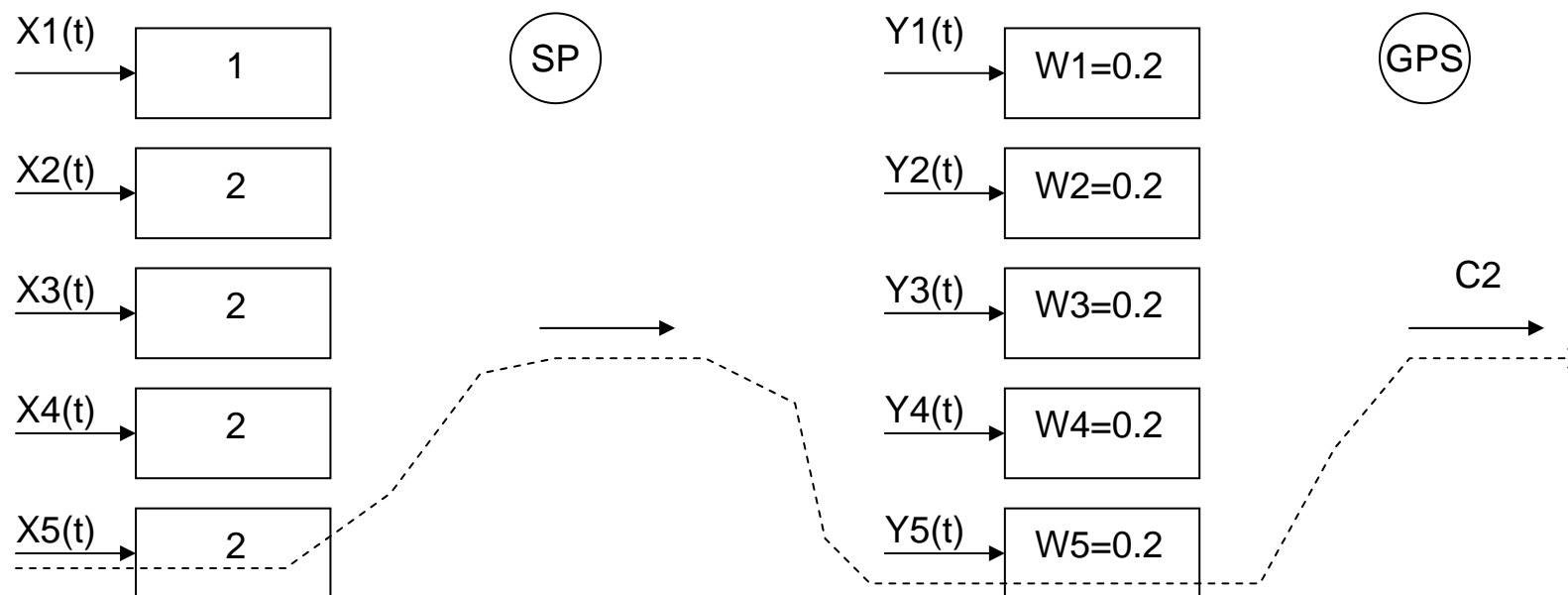


# A multihop case



{ $mX1 \rightarrow 1000000$ ,  $mX2 \rightarrow 1000000$ ,  $mX3 \rightarrow 1000000$ ,  $mX4 \rightarrow 1000000$ ,  $mX5 \rightarrow 1000000$ ,  $bX1 \rightarrow 1000000$ ,  $bX2 \rightarrow 1000000$ ,  $bX3 \rightarrow 1000000$ ,  $bX4 \rightarrow 1000000$ ,  $bX5 \rightarrow 1000000$ ,  
 $mY1 \rightarrow 1000000$ ,  $mY2 \rightarrow 1000000$ ,  $mY3 \rightarrow 1000000$ ,  $mY4 \rightarrow 1000000$ ,  $bY1 \rightarrow 1000000$ ,  $bY2 \rightarrow 1000000$ ,  $bY3 \rightarrow 1000000$ ,  $bY4 \rightarrow 1000000$ ,  $w1 \rightarrow 0.2$ ,  $w2 \rightarrow 0.2$ ,  $w3 \rightarrow 0.2$ ,  
 $w4 \rightarrow 0.2$ ,  $w5 \rightarrow 0.2$ ,  $C2 \rightarrow 25000000$ ,  $d \rightarrow 0.05$ ,  $HX1 \rightarrow 0.85$ ,  $HX2 \rightarrow 0.85$ ,  $HX3 \rightarrow 0.85$ ,  $HX4 \rightarrow 0.85$ ,  $HX5 \rightarrow 0.85$ ,  $HY1 \rightarrow 0.85$ ,  $HY2 \rightarrow 0.85$ ,  $HY3 \rightarrow 0.85$ ,  $HY4 \rightarrow 0.85$ }

Calculate the probability that the delay of flow  $Y5(t)$  exceeds 0.05 s in the GPS scheduler

# A multihop case

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$$\begin{aligned} E(X_1(t)) &= m_{X_1} t & \text{var}(X_1(t)) &= m_{X_1} b_{X_1} t^{2H_{X_1}} & E(Y_1(t)) &= m_{Y_1} t & \text{var}(Y_1(t)) &= m_{Y_1} b_{Y_1} t^{2H_{Y_1}} \\ E(X_2(t)) &= m_{X_2} t & \text{var}(X_2(t)) &= m_{X_2} b_{X_2} t^{2H_{X_2}} & E(Y_2(t)) &= m_{Y_2} t & \text{var}(Y_2(t)) &= m_{Y_2} b_{Y_2} t^{2H_{Y_2}} \\ E(X_3(t)) &= m_{X_3} t & \text{var}(X_3(t)) &= m_{X_3} b_{X_3} t^{2H_{X_3}} & E(Y_3(t)) &= m_{Y_3} t & \text{var}(Y_3(t)) &= m_{Y_3} b_{Y_3} t^{2H_{Y_3}} \\ E(X_4(t)) &= m_{X_4} t & \text{var}(X_4(t)) &= m_{X_4} b_{X_4} t^{2H_{X_4}} & E(Y_4(t)) &= m_{Y_4} t & \text{var}(Y_4(t)) &= m_{Y_4} b_{Y_4} t^{2H_{Y_4}} \\ E(X_5(t)) &= m_{X_5} t & \text{var}(X_5(t)) &= m_{X_5} b_{X_5} t^{2H_{X_5}} & & & & \end{aligned}$$

# A multihop case

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$$\text{var}(S_{X_5}(t)) = \text{var}(X_1(t)) + \text{var}(X_2(t)) + \text{var}(X_3(t)) + \text{var}(X_4(t))$$

$$\text{var}(Y_5(t)) = \max(\text{var}(X_5(t)), \text{var}(S_{X_5}(t)))$$

$$E(Y_5(t)) = E(X_5(t))$$

$$E(S_{Y_5}(t)) = w_5 C_2 t + \sum_{j=1}^4 \frac{w_5}{\sum_{k=1 \dots 5, k \neq j} w_k} (w_j C_2 t - E(X_j(t)))$$

# A multihop case

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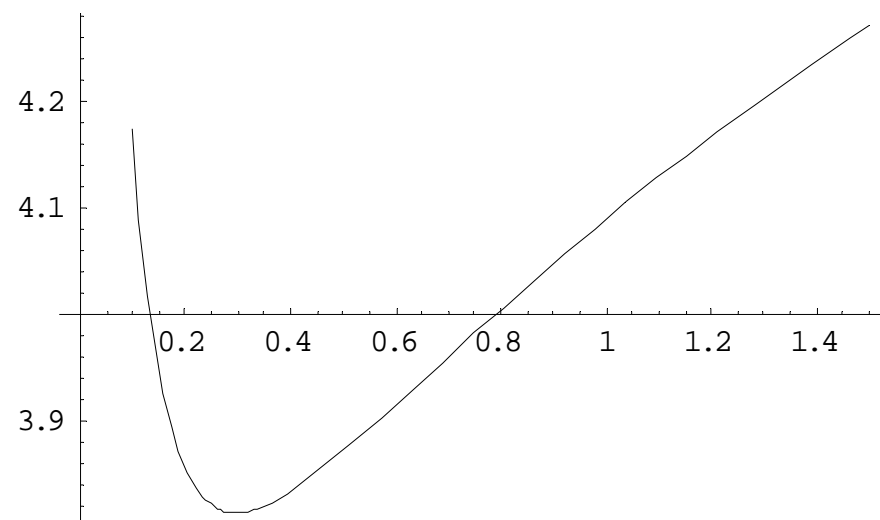
$$\text{var}(S_{Y_5}(t)) = \sum_{j=1}^4 \left( \frac{w_5}{\sum_{k \neq j} w_k} \right)^2 \text{var}(X_j(t))$$

$$\alpha(t) = - \frac{E(Y_5(t)) - E(S_{Y_5}(t+d))}{\sqrt{\text{var}(Y_5(t)) + \text{var}(S_{Y_5}(t+d))}}$$

$$\alpha(t) = \frac{-1 \times 10^6 t + 9 \times 10^6 (t + 0.05)}{\sqrt{2.5 \times 10^{11} (t + 0.05)^{1.7} + 4 \times 10^{12} t^{1.7}}}$$

# A multihop case

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$$\Pr(D > 0.05) = e^{-\frac{\alpha_{\min}^2}{2}} = 6.9 \times 10^{-4}$$